Lecture 10: Stable age structures

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Outline

- Age pyramids
- Stable population

Age pyramids

- There is theory to deal with age structure
  - It accounts for the relative numbers of young and old men and women in a population
- Basic idea is to obtain formulas for how a population will be theoretically distributed by age
  - If population has been closed to migration
  - If its birth and death rates have been unchanging for a long time

Actual ≠ Theoretical

- The actual age distribution of the population naturally differs from the theoretical age distribution

- Deviations are explained by
  - Events of migration
  - Changes in rates in the prior history of the population

General and special features

- The age distribution of each population has
- General features
  - Which it shares with populations with the same vital rates
- Special features
  - Which are derived from its own particular history

Graphical diagrams

- Age pyramid, age distribution, age structure
  - They represent the distribution of the population by age and sex
  - They are made up of a pair of bar graphs, one for men and one for women, turned on their sides and joined
- The vertical axis corresponds to age
  - The young are toward the bottom, the elderly toward the top
  - The open-ended age group at the very top is sometimes drawn with a triangle instead of bars
- For each age group
  - The bar coming off the axis to the right represents the number of women in that age group
  - The bar to the left the number of men

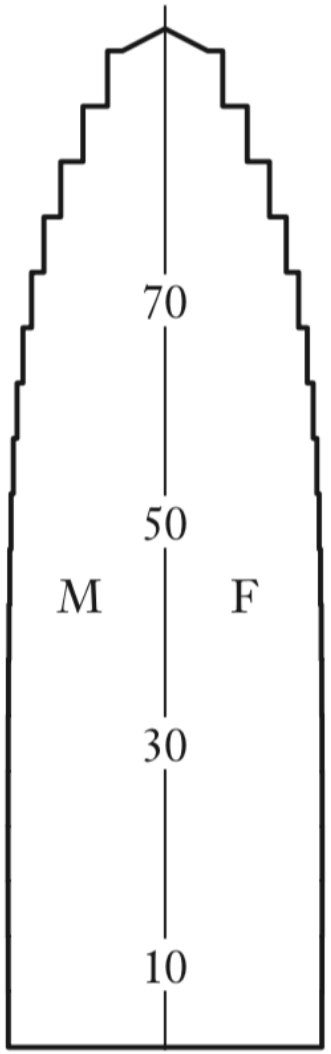
Idealized age pyramids

- Examples of idealized stable pyramids that occur in closed populations with unchanging vital rates

- Tall and slender
  - It is a case for a long-lived population with near zero growth

- Quite pyramidal in shape
  - It is a case for a population with heavy mortality and rapid growth

Tall and slender



Quite pyramidal in shape

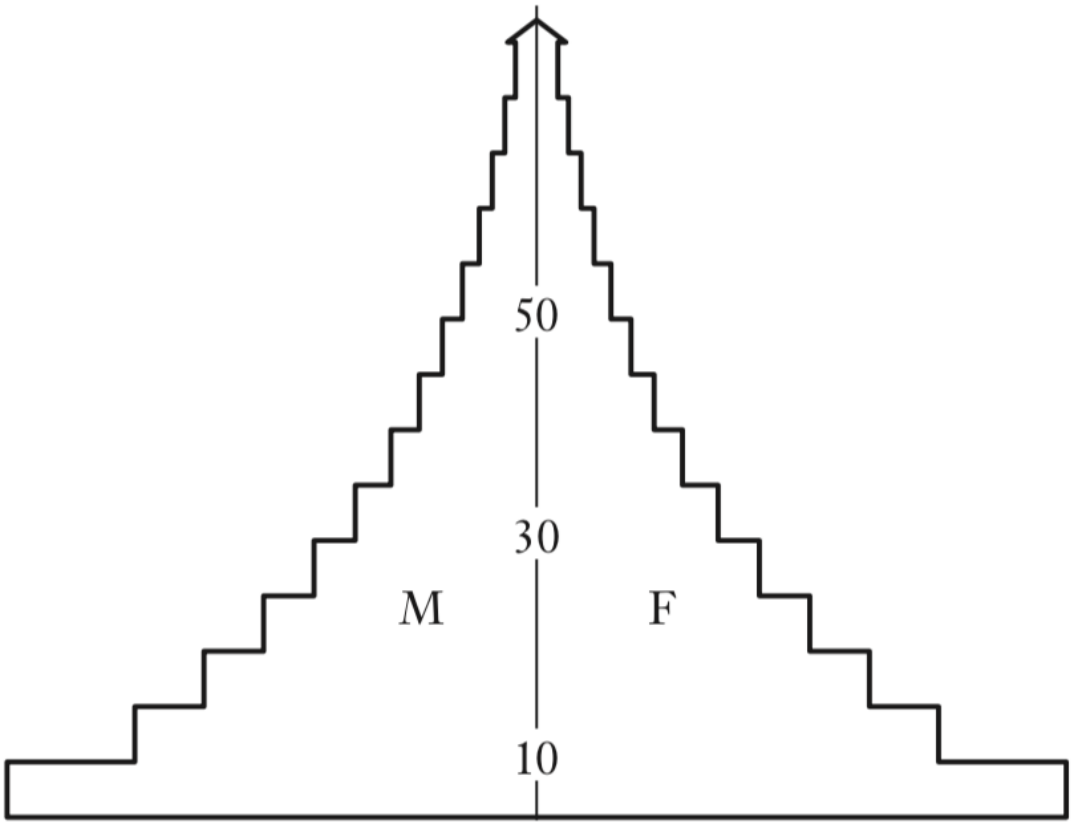
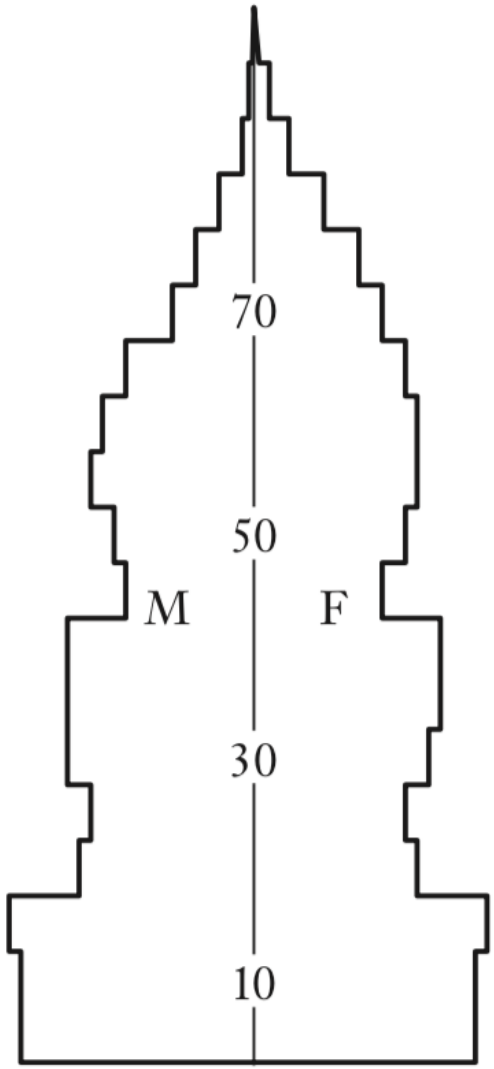


Figure 10.1 Examples of stable age pyramids

Observed age pyramids

- Examples of observed age pyramids
- France in 1960
  - It shares overall shape with the low-growth sable case
  - But notches among 20 and 40 years of age due to low births during World Wars I and II
- Mauritius in 1963
  - It shares overall shape with high-growth stable case
  - But indentations at working ages hint at changes around 1945 from increasing growth
    - Gains against infant mortality

France, 1960



Mauritius, 1963

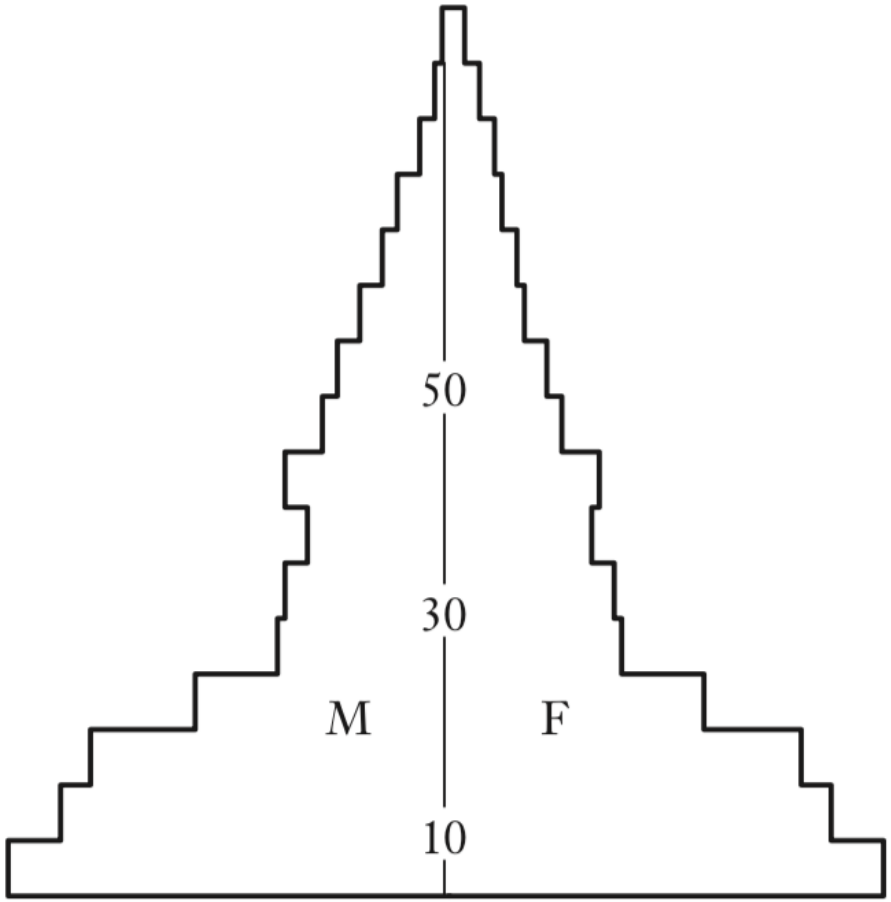
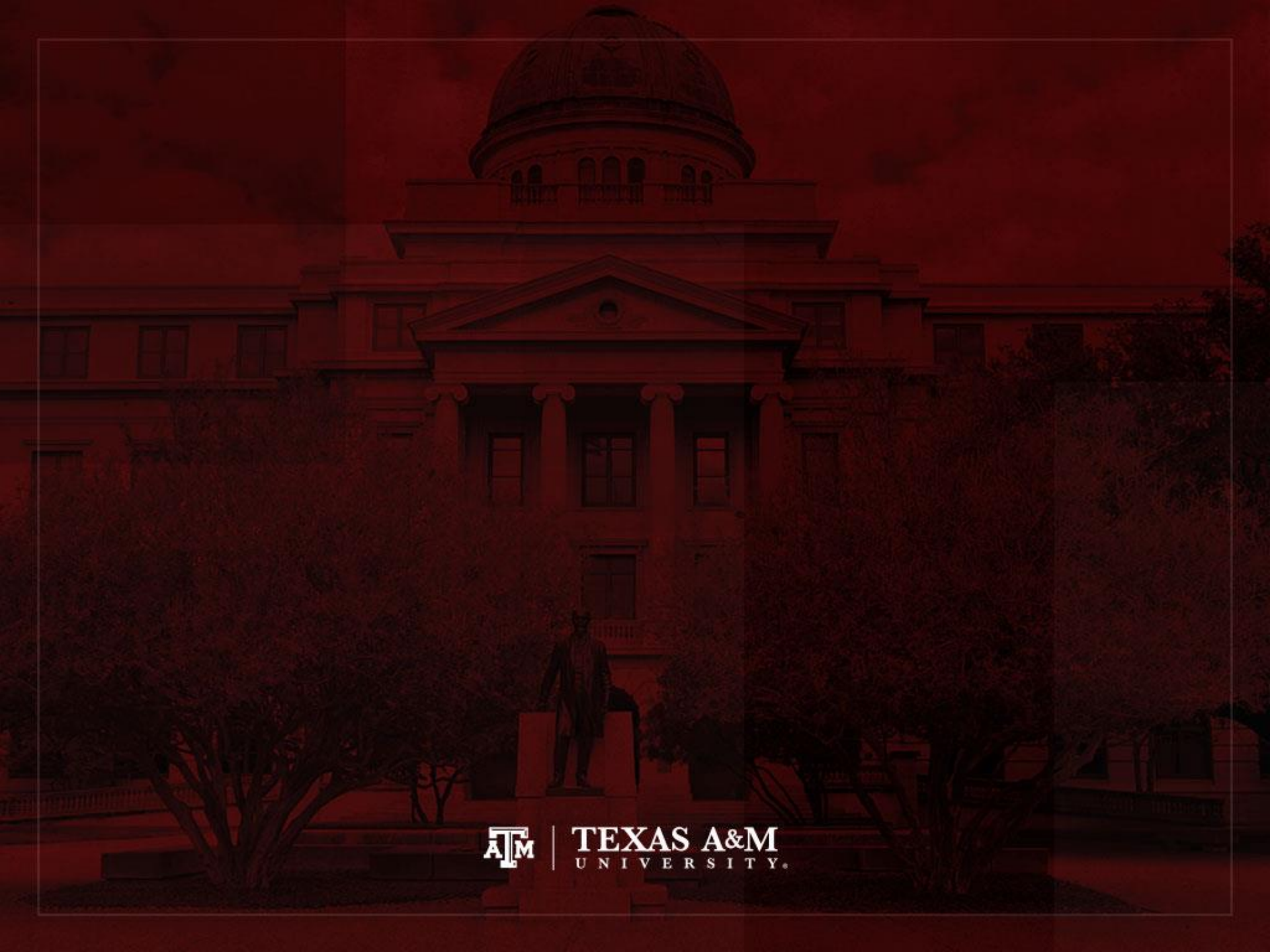


Figure 10.2 Examples of observed age pyramids

Idealized ≠ Observed

- Stable theory captures general features well
- Observable differences from stable shapes due to each nation's own history
  - Changing rates
  - Movements across borders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Stable population

- Stable population is any population produced by age-specific rates of fertility and mortality constant over a long period of time
  - Its age pyramid is determined uniquely by its lifetable and its long-term growth rate
  - Proportions in each age group in a stable population do not change over time
  - Numbers in each age group may change over time
    - Population may be growing or declining in size
    - It depends on what the growth rate happens to be

Stable population theory

- Stable population theory is the mathematical analysis of stable age pyramids
- It is a theory that goes back to the work of Leonhard Euler in 1760
- It was extensively developed by
  - Alfred Lotka in the early 1900s
  - Nathan Keyfitz and Ansley Coale in the last half-century

Stable population

- Alfred Lotka (1880–1949) used life tables in the development of his stable population theory

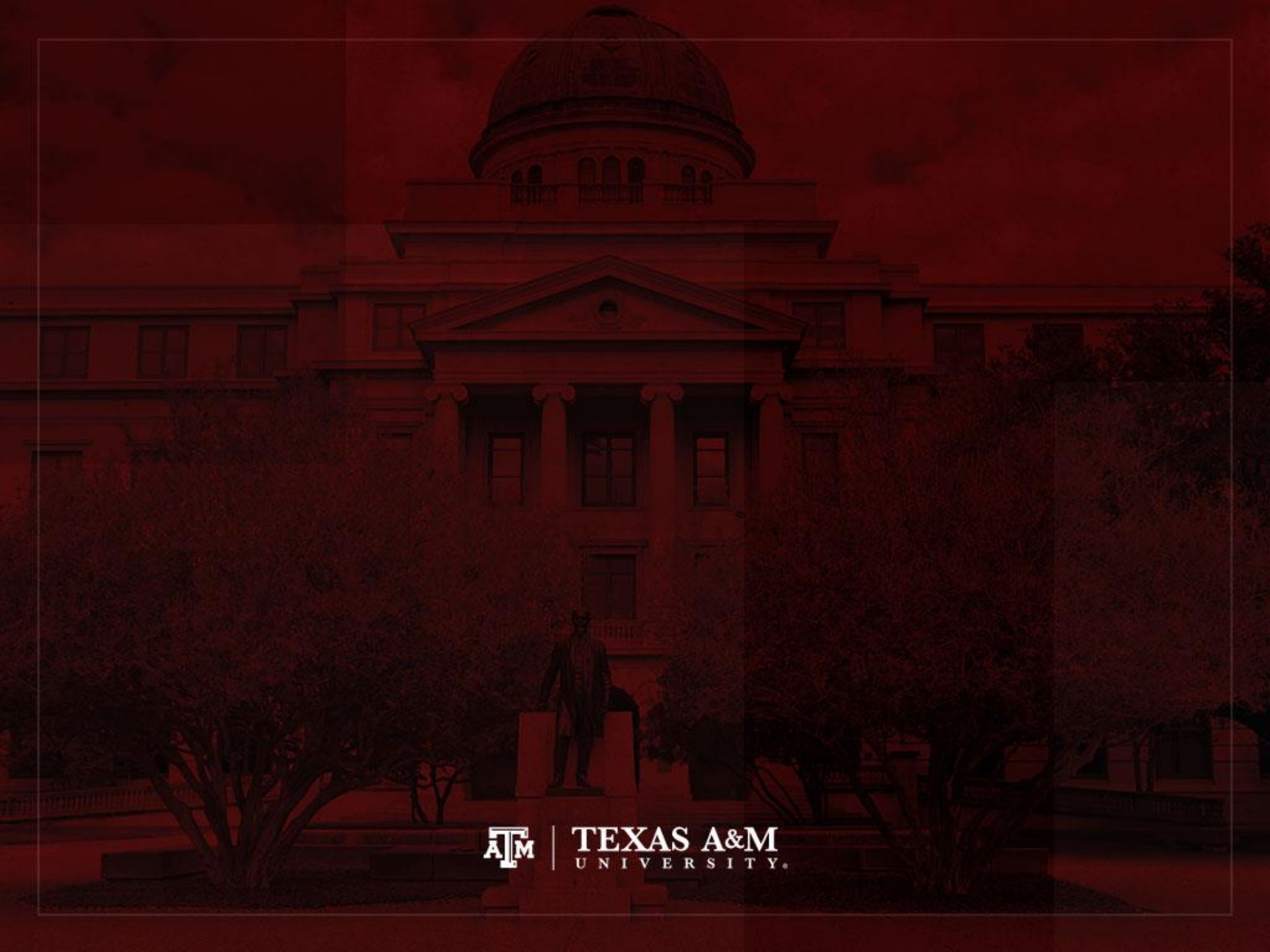
- If a population that is closed to migration experiences constant schedules of age-specific fertility and mortality rates
  - It will develop a constant age distribution
  - It will grow at a constant rate, irrespective of its initial age distribution

Stable population theory

- It considers a closed population
  - A population in which migration does not occur
- If a population experiences constant age-specific fertility and mortality rates for a long time
  - It develops a constant age distribution and grows at a constant rate, irrespective of its initial age distribution
  - Demographers sometimes indicate that stable populations forget their past
- Age distribution of a stable population depends on
  - The underlying age-specific mortality rates
  - The rate of growth

References

Wachter KW. 2014. Essential Demographic Methods. Cambridge: Harvard University Press. Chapter 10 (pp. 218–249).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